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VI Semester B.Sc. Degree (CBCSS-Reg./Supple./Improv.)
Examination, April 2020
(2014 Admission Onwards)
CORE COURSE IN MATHEMATICS
6B10MAT: Linear Algebra

Time: 3 Hours Max. Marks: 48

SECTION - A

All the first 4 questions are compulsory. They carry 1 mark each.

- Give an example to show that if f and g are two quadratic polynomials then the polynomial f + g need not be quadratic.
- 2. Obtain a basis for Mag (R).
- Let V = P₂ (R) and let β = {1, x, x²} be the standard ordered basis for V. If f(x) = 3x² + 2x + 1 then [f]_a is
- 4. Give the nature of characteristic roots of
 - i) a Hermitian matrix and
 - ii) a Unitary matrix.

SECTION - B

Answer any 8 questions from among the questions 5 to 14. These questions carry 2 marks each.

- 5. Find the equation of the line through the points P (2, 0, 1) and Q (4, 5, 3).
- 6. What is the possible difference between a generating set and a basis ?
- Is the union of two subspaces W₁ and W₂ of a vectorspace V again a subspace of V ? Justify with an example.

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- Let V be a vectorspace and β = (x₁, x₂, ..., x_n) be a subset of V. Show that β is basis if each vector y in V can be uniquely expressed as a linear combination of vectors in β.
- Show that T: R^p → R² defined by T (a₁, a_p) = (2a₁ + a₂, a₁) is a linear transformation.
- Let T: V → W be a linear transformation. Prove that N (T), the nullspace of T, is a subspace of V.
 - 11. Find a basis of the row space of the matrix

1 1 1 3 4 5 2 3 4

12. Find the characteristic values of the matrix

1 1 2 0 2 2 -1 1 3

13. Use Gauss elimination to solve the system of equations :

10x + y + z = 12

2x + 10y + z = 13

x + y + 3z = 5.

14. Use Gauss, Jordan elimination to solve the system of equations :

10x + y + z = 12

2x + 10y + z = 13

x + y + 3z = 5.





SECTION - C

Answer any 4 questions from among the questions 15 to 20. These questions carry 4 marks each.

15. In every vectorspace V over a field F prove that

i) a0 = 0 ∀a ∈ F, where 0 is the zero vector and

ii) $(-a)x = -(ax) \forall a \in F \text{ and } \forall x \in V.$

Define linear dependence and linear independence of vectors with examples.

 Define a linear transformation from a vectorspace V into W. Verify that T: M_{most} → M_{nom} by T (A) = A' where A' is the transpose of A, is linear.

18. Show that the row nullity and column nullity of a square matrix are equal.

 Find the characteristic values and the corresponding characteristic vectors of the matrix.

2 1 0 0 2 1 0 0 2

20. Use the Gaussian elimination method to find the inverse of the matrix.

2 1 1 3 2 3 1 4 9

SECTION - D

Answer any 2 questions from among the questions 21 to 24. These questions carry 6 marks each.

If a vectorspace V is generated by a finite set S_o, then show that a subset of S_o is a basis for V and V has a finite basis.

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- 22. State and prove dimension theorem. Deduce that a linear transformation T: V → V is one to one if and only if T is onto.
- 23. Show that the matrix

$$A = \begin{bmatrix} 0 & 0 & 1 \\ 3 & 1 & 0 \\ -2 & 1 & 4 \end{bmatrix}$$

satisfies Cayley Hamilton theorem and hence obtain A-1.

24. Prove that

$$A = \begin{bmatrix} 4 & 0 & 1 \\ 2 & 3 & 2 \\ 1 & 0 & 4 \end{bmatrix}$$

is diagonalizable and find the diagonal form.