K23U 0518
Reg. No. : $\qquad$
Name: $\qquad$

# VI Semester B.Sc. Degree (CBCSS - OBE-Regular/Supplementary/ Improvement) Examination, April 2023 <br> (2019 and 2020 Admissions) DISCIPLINE SPECIFIC ELECTIVE IN MATHEMATICS <br> 6B14BMAT : Operations Research 

Time : 3 Hours
Max. Marks : 48

## SECTION - A

Answer any 4 questions out of 5 questions. Each question carries 1 mark.

1. Define convex set.
2. Define a balanced transportation problem.
3. Write the basic terms used in sequencing problem.
4. State the max-min principle.
5. Define degenerate solution of an LPP.

## SECTION - B

Answer any 8 questions out of 11 questions. Each question carries $\mathbf{2}$ marks.
6. Write the quadratic form $x_{1}^{2}+8 x_{1} x_{2}+16 x_{2}^{2}-3 x_{3}^{2}$ in the form $x^{\top} A x$.
7. Write the procedure for graphical method in linear programming problem.
8. Write the dual of the linear programming problem

Maximize $Z=4 x_{1}+2 x_{2}$
subject to $x_{1}+x_{2} \geq 3, x_{1}-x_{2} \geq 2, x_{1}, x_{2} \geq 0$.
9. Explain North West Corner method.
10. Explain duality in transportation problem.
11. Explain mathematical formulation of Assignment problem.
12. Write the optimal sequence algorithm for n jobs on k machines.
13. Explain maintenance crew scheduling.
14. Write the rules for determining a saddle point.
15. Explain pure strategy and mixed strategy.
16. Define standard form of an LPP.

## SECTION - C

Answer any 4 questions out of 7 questions. Each question carries 4 marks.
17. Determine whether the quadratic form $x_{1}^{2}+2 x_{2}^{2}+2 x_{3}^{2}-2 x_{1} x_{2}-2 x_{2} x_{3}$ is positive definite.
18. An animal feed company must produce 200 lbs of a mixture containing the ingredients $X_{1}$ and $X_{2} \cdot X_{1}$ costs Rs. 3 per lbs and $X_{2}$ costs Rs. 8 per Ibs. Not more than 80 lbs of $X_{1}$ can be used and minimum quantity to be used for $X_{2}$ is 60 lbs . Find how much of each ingredient should be used if the company wants to minimize the cost. Formulate the problem mathematically.
19. Obtain an initial basic feasible solution using least cost method.

|  | $\mathbf{D}_{1}$ | $\mathrm{D}_{2}$ | $\mathrm{D}_{3}$ | $\mathrm{D}_{4}$ | Capacity |
| :--- | :---: | :---: | :---: | :---: | :---: |
| $\mathbf{O}_{1}$ | 1 | 2 | 3 | 4 | 6 |
| $\mathbf{O}_{2}$ | 4 | 3 | 2 | 0 | 8 |
| $\mathbf{O}_{3}$ | 0 | 2 | 2 | 1 | 10 |
| Demand | 4 | 6 | 8 | 6 |  |

20. Write the algorithm to compute the initial basic feasible solution using VAM.
21. A department head has four tasks to be performed and three subordinates, the subordinates differ in efficiency. The estimates of time each subordinate would take to perform, is given below in the matrix. How should he allocate the tasks one to each man, so as to minimize the total man hours ?

| Task | Men |  |  |
| :---: | :---: | :---: | :---: |
|  | $\mathbf{1}$ | $\mathbf{2}$ | $\mathbf{3}$ |
| I | $\mathbf{9}$ | 26 | 15 |
| II | 13 | 27 | 6 |
| III | 35 | 20 | 15 |
| IV | 18 | 30 | 20 |

22. Solve the following sequencing problem when passing out is not allowed.

| Item | Machine (Processing time in <br> hours) |  |  |  |
| :---: | :---: | :---: | :---: | :---: |
|  | A | B | C | D |
| I | 15 | 5 | 4 | 15 |
| II | 12 | 2 | 10 | 12 |
| III | 16 | 3 | 5 | 16 |
| IV | 17 | 3 | 4 | 17 |

23. Solve the following 2 person zero sum game.

## Player B

## Player A

10
6
4

5
7
8
$-2$
3
4
$(4 \times 4=16)$
SECTION - D

Answer any two questions out of 4 questions. It carries 6 marks.
24. Use simplex method to maximize $Z=x_{1}+2 x_{2}+3 x_{3}$

$$
\begin{array}{ll}
\text { subject to } & x_{1}+2 x_{2}+3 x_{3} \leq 10, \\
& x_{1}+x_{2} \leq 5 \\
& x_{1}, x_{2}, x_{3} \geq 0 .
\end{array}
$$

25. Solve the following transportation problem.

| From | To |  |  | Available |
| :---: | :---: | :---: | :---: | :---: |
|  | A | B | C |  |
| I | 6 | 8 | 4 | 14 |
| II | 4 | 9 | 8 | 12 |
| III | 1 | 2 | 6 | 5 |
| Requirement | 6 | 10 | 15 |  |

26. Write the optimum sequence algorithm for $n$ jobs on 2 machines.
27. Solve the following $2 \times 2$ game graphically.

Player B

Player A


